

TAMIL NADU OPEN UNIVERSITY

Chennai - 15 School of Science

ASSIGNMENT

Programme Code No : 131

Programme Name : B.Sc., Mathematics

Course Code & Name : BMSS-21, Differential Calculus

Batch : AY 2022-23(1^{rst} year)

No.of Assignment : One Assignment for Each 2 Credits

Maximum Marks : 30(Average of Total NO .Of Assignments)

Assignment - I

Max.: 30 Marks

Answer any ONE of the question not exceeding 1000 words

1. (a) Find
$$\frac{d^2y}{dx^2}$$
 if $y = (2x+1)\tan^{-1}x$

(b) If
$$xy = ae^x + be^x$$
 prove that $x\frac{d^2y}{dx^2} + 2\frac{dy}{dx}xy = 0$

2. (a) Investigate the maximum and minimum value of

$$4x^2 + 6xy + 9y^2 + 8x + 24y + 4$$

(b) Using Lagrange's Multipliers nd the maximum and minimum value of

$$f(x, y, z) = x + y + z$$
 subject to $\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 1$

3. (a) Find the envelope of the family of lines $\frac{x}{a} + \frac{y}{b} = 1$ where a & b the parameters a and b are connected by the relation $a^n + b^n = c^n$

(b) Find the radius of curvature of the curve $xy^2 = a^3x^3$ at the point (a,0).